

WORKSHEET: PROBABILITY

NAME: _____

CLASS: _____

DATE: {1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20}

Question 1

A bag contains 20 balls which are numbered from 1 to 20. Find the probability of drawing at random, a ball that is

- an even number,
- greater than 5 but smaller than 12,
- a prime number,
- not a prime number.

Answer: $P(\text{even}) = \frac{1}{2}$
 Answer: $P(5 < N < 12) = \frac{6}{20} = \frac{3}{10}$
 Answer: $P(\text{prime}) = \frac{8}{20} = \frac{2}{5}$
 Answer: $P(\text{not prime}) = \frac{3}{5}$

Question 2

A two-digit number is formed at random using the digits 2, 3, 4 and 5 with repetition of digits allowed.

- List the sample space.
- Find the probability of
 - forming an odd number,
 - forming a number x , where $x > 44$,
 - forming a number divisible by 5.

Answer: {22, 23, 24, 25, 32, 33, 34, 35, 42, 43, 44, 45, 52, 53, 54, 55}

Answer: $P(\text{odd}) = \frac{1}{2}$
 Answer: $P(x > 44) = \frac{5}{16}$
 Answer: $P(\div 5) = \frac{4}{16} = \frac{1}{4}$

Question 3

A box contains 30 apples, of which 14 are red and 16 are green. An apple is picked at random from the box.

- Find
- the probability of picking a green apple,
 - the number of red apples to be removed so that the probability of picking a green apple from the remaining apples in the box is $\frac{2}{3}$.

Answer: $P(\text{Green}) = \frac{16}{30} = \frac{8}{15}$

let $x \rightarrow$ be apples removed
 Answer: $P(\text{Green, After}) = \frac{16}{30-x} = \frac{2}{3} = \frac{16}{24}$
 $x = 6$

Question 4

A box contains 2 blue balls, 2 red balls and 1 green ball. A second box contains 1 red toy block, 1 green toy block and 1 yellow toy block. A ball and a toy block are drawn at random from their respective boxes.

	Blue	Blue	Red	Red	Green
Red	B, R	B, R	R, R	R, R	G, R
Green	B, G	B, G	R, G	R, G	G, G
Yellow	B, Y	B, Y	R, Y	R, Y	G, Y

$n(S) = 15$

- Complete the possibility diagram above.
- Find the probability that the ball and toy block
 - are both red in colour,
 - have the same colours,
 - have different colours.

Answer: $P(RR) = \frac{2}{15}$
 Answer: $P(\text{same}) = \frac{3}{15} = \frac{1}{5}$
 Answer: $P(\text{diff. colour}) = \frac{4}{5}$

Question 5

A letter is selected at random from each of the two words 'EARTH' and 'MARS'.

(a) Complete the possibility diagram below showing all the possible outcomes.

	E	A	R	T	H
M	✓	✓			
A	✓	✓✓	✓	✓	✓
R	✓	✓	✓		
S	✓	✓			

$n(S) = 20$

(b) Find the probability that

(i) the two letters are the same,

Answer: $P(\text{same}) = 2/20 = 1/10$

(ii) at least one of the two letters is a vowel.

Answer: $P(\text{at least one vowel}) = 11/20$

Question 6

A box contains x red balls, $(x + 3)$ blue balls and $(3x - 1)$ white balls.

(a) If the probability of drawing a red ball is $2/11$, find the value of x .

$\frac{3x-1}{x+3} = \frac{2}{11}$

$P(\text{red}) = \frac{x}{5x+2} = \frac{2}{11}$
 $11x = 10x + 4$
 $x = 4$

Answer: $x = 4$

(b) Find the probability of a white ball.

Answer: $P(\text{white}) = 11/22 = 1/2$

Question 7

There are 5 discs in a bag, labelled with numbers from 3 to 7. Two discs are drawn at random, one at a time without replacement, from the bag. The possibility diagram below shows the product of the two numbers.

×	3	4	5	6	7
3		12 ✓	15 ✓	18 ✓	21
4	12 ✓		20 ✗	24	28
5	15 ✓	20 ✗		30 ✗	35 ✓
6	18 ✓	24	30 ✗		42 ✓
7	21	28	35 ✓	42 ✓	

Find the probability that the product of the two numbers is

(a) an odd number,

Answer: $P(\text{odd}) = 6/20 = 3/10$

(b) a multiple of 10,

Answer: $P(10) = 4/20 = 1/5$

(c) less than 20 OR more than 30.

Answer: $P(< 20 \text{ or } > 30) = 10/20 = 1/2$

Question 8

A card is taken from a well-shuffled standard pack of 52 cards. Find the probability that it is

(a) an ace of clubs,

Answer: $P(\text{Ace of Clubs}) = 1/52$

(b) a king, a queen or a jack,

Answer: $P(\text{K or Q or J}) = 12/52 = 3/13$

(c) a red eight,

Answer: $P(\text{red 8}) = 2/52 = 1/26$

(d) a heart or a queen,

Answer: $P(\text{H or Q}) = \frac{13+3}{52} = 16/52 = 4/13$

(e) a black picture card or a five

Answer: $P(\text{BPC or 5}) = 10/52 = 5/26$

